## **Knight Foundation School of Computing and Information Sciences**

#### Course Title: Discrete Structures

Date: 3/12/2020

#### Course Number: COT 3100

#### Number of Credits: 3

Subject Area: Foundations	Subject Area Coordinator: Hadi Amini		
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<b>Catalog Description:</b> Align mathematical and computational concepts by applying computing to propositional logic, sets, functions, relations, induction, recursion, combinatorics, Boolean algebra, graph and trees.			
<b>Textbook:</b> Susanna S. Epp, Discrete Mathematics with Applications, 4 <sup>th</sup> Edition, Brooks Cole, 2010, 978-0495391326			
References: MIT OpenCourseWare Mathematics for Computer Science			
<b>Prerequisites Courses:</b> MAC-XXXX and COP-XXXX (passed at least one college level math course and one basic college level programming			
Corequisite Courses: <u>COP 2210</u> or <u>COP 2250</u> or <u>EEL 2880</u>			

Type: Required for CS and IT Majors.

This course is acceptable as an alternative to MAD-2104 for CS majors and to MAD-1100 for IT majors, and satisfies the discrete requirement.

Prerequisites Topics:

- 1. Solve algebraic equations
- 2. Selection statements
- 3. Iteration
- 4. Encapsulation using functions
- 5. Writing programs that use selection, iteration and encapsulation

Discrete structures course requires that students must have completed some introductory math (any MAC-XXXX) and some introductory programming experience (any COP-XXXX) as prerequisite. Additionally, the students need university level programming experience (beyond the introductory programming course such as COP-1000) to comprehend the second half of the Discrete Structures course. For this reason, the students must have either completed or currently enrolled in COP-2210 or COP-2250 or EEL-2880.

Course Outcomes:

- 1. Master definitions and theorems involving sets, relations and functions.
- 2. Be familiar with propositional logic.
- 3. Be familiar with mathematical reasoning, including mathematical induction and recursion.
- 4. Be exposed to combinatorics.
- 5. Be familiar with graph theory.
- 6. Be exposed to Boolean Algebras.
- 7. Be exposed to computational implementations of topics covered in the other outcomes.

#### **Relationship between Course Outcomes and Program Outcomes**

BS in CS: Program Outcomes	<b>Course Outcomes</b>
a) Demonstrate proficiency in the foundation areas of Computer Science including mathematics, discrete structures, logic and the theory of algorithms	1, 2, 3, 4, 5, 6
b) Demonstrate proficiency in various areas of Computer Science including data structures and algorithms, concepts of programming languages and computer systems.	
c) Demonstrate proficiency in problem solving and application of software engineering techniques	
d) Demonstrate mastery of at least one modern programming language and proficiency in at least one other.	
e) Demonstrate understanding of the social and ethical concerns of the practicing computer scientist.	
f) Demonstrate the ability to work cooperatively in teams.	
g) Demonstrate effective communication skills.	

# Assessment Plan for the Course & how Data in the Course are used to assess Program Outcomes

Student and Instructor Course Outcome Surveys are administered at the conclusion of each offering, and are evaluated as described in the School's Assessment Plan: https://abet.cs.fiu.edu/csassessment/

Outline			
	Торіс	Number	Outcome
	_	of Lecture	
		Hours	
1.	Sets, Relations, and Functions	10	1,7
	1.1. Operations on sets		
	1.2. Equivalence relations		
	1.3. Cardinality		
2.	Logic and Mathematical Reasoning	10	2, 3, 7
	2.1. Propositional logic		
	2.2. Mathematical induction and recursion		
3.	Combinatorics	5	4, 7
	3.1. Combinatorial identities		
	3.2. Binomial theorem		
4.	Directed and Undirected Graphs	10	5,7
	4.1. Isomorphism of graphs		
	4.2. Paths		
	4.3. Adjacency matrices		
	4.4. Euler paths		
	4.5. Four-color problem		
	4.6. Planar graphs		
	4.7. Trees and tree traversal		
_			< <b>7</b>
5.	<u>Boolean Algebras</u>	5	6, /
	5.1. Disjunctive normal form		
	5.2. Minimization of Boolean functions (Karnaugh		
	maps)		
1		1	

## Outline

#### **Learning Outcomes**: (Familiarity $\rightarrow$ Usage $\rightarrow$ Assessment)

Sets, Relations, and Functions:

- 1. Explain with examples the basic terminology of functions, relations, and sets. [Familiarity]
- 2. Perform the operations associated with sets, functions, and relations. [Usage]
- 3. Relate practical examples to the appropriate set, function, or relation model, and interpret the associated operations and terminology in context. [Assessment]
- 4. Describe how constructs of a chosen language (e.g., Java) are used to implement sets, functions, and relations. [Assessment]

Basic Logic:

- 1. Convert logical statements from informal language to propositional and predicate logic expressions. [Usage]
- 2. Apply formal methods of symbolic propositional and predicate logic, such as calculating validity of formulae and computing normal forms. [Usage]
- 3. Use the rules of inference to construct proofs in propositional and predicate logic. [Usage]
- 4. Describe how symbolic logic can be used to model real-life situations or applications, including those arising in computing contexts such as software analysis (e.g., program correctness), database queries, and algorithms. [Usage]
- 5. Apply formal logic proofs and/or informal, but rigorous, logical reasoning to real problems, such as predicting the behavior of software or solving problems such as puzzles. [Usage]
- 6. Describe the strengths and limitations of propositional and predicate logic. [Familiarity]
- 7. Convert logical statements from informal language to propositional and predicate logic expressions and then to selection statement syntax into a programming language of choice. [Implementation]

Mathematical Reasoning:

- 1. Identify the proof technique used in a given proof. [Familiarity]
- 2. Outline the basic structure of each proof technique (direct proof, proof by contradiction, and induction) described in this unit. [Usage]
- 3. Apply each of the proof techniques (direct proof, proof by contradiction, and induction) correctly in the construction of a sound argument. [Usage]
- 4. Determine which type of proof is best for a given problem. [Assessment]
- 5. Explain the parallels between ideas of mathematical and/or structural induction and recursively defined structures. [Assessment]
- 6. Explain the relationship between weak and strong induction and give examples of the appropriate use of each. [Assessment]
- 7. Identify and trace recursion within a programming language of choice (e.g., Java). [Usage]
- 8. Determine if iteration or recursion are best for a given problem.

Combinatorics:

1. Apply counting arguments, including sum and product rules, inclusion-exclusion principle and arithmetic/geometric progressions. [Usage]

- 2. Apply the pigeonhole principle in the context of a formal proof. [Usage]
- 3. Compute permutations and combinations of a set, and interpret the meaning in the context of the particular application. [Usage]
- 4. Map real-world applications to appropriate counting formalisms, such as determining the number of ways to arrange people around a table, subject to constraints on the seating arrangement, or the number of ways to determine certain hands in cards (e.g., a full house). [Usage]
- 5. Solve a variety of basic recurrence relations. [Usage]
- 6. Analyze a problem to determine underlying recurrence relations. [Usage]
- 7. Perform computations involving modular arithmetic. [Usage]
- 8. Describe how a programming language of choice (e.g., Java) could be used to create all ordered pairs from two sets. [Assessment]

Graphs and Trees:

- 1. Illustrate by example the basic terminology of graph theory, as well as some of the properties and special cases of each type of graph/tree. [Familiarity]
- 2. Describe how to traverse trees and graphs. [Usage]
- 3. Model a variety of real-world problems in computer science using appropriate forms of graphs and trees, such as representing a network topology or the organization of a hierarchical file system. [Usage]
- 4. Show how concepts from graphs and trees appear in data structures, algorithms, proof techniques (structural induction), and counting. [Usage]
- 5. Explain how to construct a spanning tree of a graph. [Usage]
- 6. Determine if two graphs are isomorphic. [Usage]

Outcome	Number of Weeks
Sets and functions computational implementations: outcomes 1,7	3
Complex selection computational implementations: outcomes 2,7	2
Recursive computational implementations: outcomes 3,7	2
Permutation computational implementations: outcomes 4,7	2
Graph traversal program: outcomes 5,7	3
Boolean statements computational implementation: outcomes 6,7	1

#### **Course Outcomes Emphasized in Laboratory Projects / Assignments**

## **Oral and Written Communication**

No significant coverage

Written Reports		<b>Oral Presentations</b>	
Number	Approx. Number	Number	Approx. Time for
Required	of pages	Required	each
0	0	0	0

## **Social and Ethical Implications of Computing Topics**

No significant coverage

Topic Class time		student performance measures	

### Approximate number of credit hours devoted to fundamental CS topics

Fundamental CS Area	<b>Core Hours</b>	Advanced Hours
Algorithms:	0.5	
Software Design:		
Computer Organization and Architecture:		
Data Structures:	0.5	
Concepts of Programming Languages		

#### **Theoretical Contents**

Торіс	Class time
Discrete structures	40 hours

#### **Problem Analysis Experiences**

#### **Solution Design Experiences**

## The Coverage of Knowledge Units within Computer Science Body of Knowledge<sup>1</sup>

Knowledge Unit	Topic	Туре	<b>Lecture Hours</b>
DS1. Functions, relations, and	1	Tier 1	10
DS2. Basic logic	2.1, 5	Tier 1	10
DS3. Proof techniques	2.2	Tier 1	5
DS4. Basics of counting	3	Tier 1	5
DS5. Graphs and trees	4	Tier 1	10

<sup>1</sup>See Appendix A in Computer Science Curricula 2013. Final Report of the IEEE and ACM Joint Task Force on Computing Curricula, available at: https://www.acm.org/binaries/content/assets/education/cs2013\_web\_final.pdf